

## Optical Fibres - Numericals

#1-8 - through recorded video  
+ pdf document

Solving now :

# (9)  $P_{in} = 2 \text{ mW}$ ,  $P_{out} = 20 \text{ } \mu\text{m}$ ,  $L = 50 \text{ km}$

$$\alpha = \frac{10}{L} \log \left( \frac{P_{in}}{P_{out}} \right); \text{ L in km}$$

$$= \frac{10}{50} \log \left( \frac{2 \times 10^{-3}}{20 \times 10^{-6}} \right)$$

$$= 0.4 \text{ dB/km}$$

$$\textcircled{10} \quad \alpha = 0.2 \text{ dB/km}, \quad L = ?$$

$$P_{\text{out}} = 10\% \text{ of } P_{\text{in}} = 0.1 P_{\text{in}}$$

$$\alpha = \frac{10}{L} \log \left( \frac{P_{\text{in}}}{P_{\text{out}}} \right)$$

$$L = \frac{10}{\alpha} \log \left( \frac{P_{\text{in}}}{0.1 P_{\text{in}}} \right) = \frac{10}{\alpha} \log(10)$$

$$\Rightarrow \alpha = \frac{10}{L} \Rightarrow L = \frac{10}{\alpha} = \frac{10}{0.2}$$

$$L = 50 \text{ km}$$

$$\textcircled{11} \quad n_1 = 1.46, \quad \Delta = 0.015, \quad L = 1500 \text{ m}$$

$$\tau_i = \frac{n_1 \Delta L}{c} = \frac{1.46 \times 0.015 \times 1500}{3 \times 10^8}$$

$$= 1.095 \times 10^{-7} \text{ s} \quad \text{or} \quad 109.5 \text{ ns}$$

$$\frac{\tau_i}{L} = \frac{n_1 \Delta}{c} = \frac{1.095 \times 10^{-7}}{1500} = 7.3 \times 10^{-11} \text{ s/m}$$

$$= 7.3 \times 10^{-11} \times 10^{12} \text{ ns/km}$$

$$= 73 \text{ ns/km}$$

(12)  $n_1 = 1.5$ ,  $\Delta = 0.01$  (graded index fibre)

$$\Delta = \frac{n_1 - n_2}{n_1} \Rightarrow n_2 = n_1(1 - \Delta)$$

$$n_2 = 1.5(1 - 0.01) = 1.485$$

$$\frac{\tau_i}{L} = \frac{n_2 \Delta^2}{2c} = \frac{1.485 \times (0.01)^2}{2 \times 3 \times 10^8}$$

$$= 2.475 \times 10^{-13} \text{ s/m}$$

$$= 2.475 \times 10^{-13} \times 10^{12} \text{ ns/km}$$

$$= 0.247 \text{ ns/km}$$

$$(13) \alpha_f = 0.2 \text{ dB/km}, L = 10 \text{ km}, P_{in} = 5 \text{ mW}, \alpha_c = 1 \text{ dB}$$

w/o connectors:

$$\alpha_f = \frac{10}{L} \log\left(\frac{P_{in}}{P_{out}}\right) \Rightarrow \frac{P_{in}}{P_{out}} = 10^{\alpha L/10}$$

$$\therefore P_{out} = \frac{P_{in}}{10^{\alpha L/10}} = \frac{5}{10^{0.2 \times 10/10}} = \frac{5}{10^{0.2}}$$

$$= 3.15 \text{ mW}$$

with connectors:

total loss factor: total loss offered by 10 km long fibre  
+ loss offered by connectors

$$\begin{aligned} \alpha_{tL} &= \alpha_f \cdot L + 2 \cdot \alpha_c \\ &= 0.2 \times 10 + 2 \times 1 \\ &= 4 \text{ dB} \quad (\text{not } \downarrow 13 / \text{Km}) \end{aligned}$$

$$\alpha_f \cdot L = 10 \log \left( \frac{P_{in}}{P_{out}'} \right)$$

$$\therefore P_{out}' = \frac{P_{in}}{10^{\alpha_{tL}/10}} = \frac{5}{10^{4/10}} = \frac{5}{10^{0.4}}$$

$$= 1.99 \approx 2 \text{ mW}$$

$$\therefore \% \text{ decrease in o/p power} = \frac{P_{out} - P_{out}'}{P_{out} \times 100} = \frac{3.15 - 2}{3.15} \times 100 = 36.5\%$$

$$\textcircled{14} \quad n_1 = 1.46, \quad n_2 = 1.42 \quad \Rightarrow \quad \Delta = \frac{n_1 - n_2}{n_1} = \frac{1.46 - 1.42}{1.46}$$

$$\tau_m = 1.7 \text{ ns/km}$$

$$L = 2 \text{ km}$$

$$= 0.027$$

$$\Rightarrow \tau_m \text{ total} = 1.7 \times 2 = 3.4 \text{ ns}$$

$$\tau_i \text{ (SI)} = \frac{n_1 L \Delta}{c} = \frac{1.46 \times 2000 \times 0.027}{3 \times 10^8} = 2.628 \times 10^{-7} \text{ s}$$
$$= 262.8 \text{ ns}$$

$$\tau_i \text{ (GRIN)} = \frac{n_2 L \Delta^2}{2c} = \frac{1.42 \times 2000 \times (0.027)^2}{2 \times 3 \times 10^8} = 3.45 \times 10^{-9} \text{ s}$$
$$= 3.45 \text{ ns}$$

total dispersion

$$\tau(\text{SI}) = \sqrt{\tau_i^2(\text{SI}) + \tau_m^2} \approx \tau_i(\text{SI}) \text{ as } \tau_i(\text{SI}) \gg \tau_m$$
$$\approx 262.8 \text{ ns}$$

$$\therefore B(\text{SI}) = \frac{0.7}{\tau} = \frac{0.7}{262.8 \times 10^{-9}} \approx 2.66 \times 10^6 \text{ bits/sec}$$
$$= 2.66 \text{ MBPS}$$

$$\tau(\text{GRIN}) = \sqrt{\tau_i^2(\text{GRIN}) + \tau_m^2} = \sqrt{3.45^2 + 3.4^2} \approx 4.84 \text{ ns}$$

$$B(\text{GRIN}) = \frac{0.7}{\tau} = \frac{0.7}{4.84 \times 10^{-9}} \approx 144.6 \times 10^6 \text{ bits/sec}$$
$$= 144.6 \text{ MBPS}$$

SM  $\rightarrow$  206 MBPS